**Week 3 – Notes**

**Neural Networks Overview**

Superscript inside square brackets represents the notation for the number of the layer

**Neural Network Representation**

Each layer, including the input and the output can be seen as activation layers

Therefore, each layer is denoted by a and a superscript inside square brackets where we put the index of the layer

A neural network that has the input, hidden and output layers is referred to as a 2 layer neural network, because the input layer is not counted

**Computing a Neural Network's Output**

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This is the representation of one unit, that can be perceived as 2 parts

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All the calculations for on layer can be computed just by multiplying the matrices

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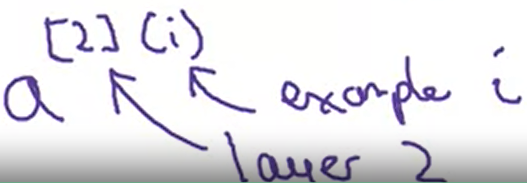
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**Vectorizing Across Multiple Examples**

If we want to compute the forward propagation for all examples, we will have to do the following computation for each training examples:

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As a notation we use 

To create a forward pass on each example of the data set we would need a for loop, but to avoid it we can vectorize the entire data set:

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Description automatically generated(create a matrix X in which we have an x on each column)

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Description automatically generated(same Z and A, where the columns stand for the examples, and the rows for hidden units)

We end up using the following computations for a vectorized forward pass across the entire data set

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Description automatically generated

When we vectorize across all examples, we have to keep in mind that during the forward pass the weights are the same for all training examples

**Activation Functions**

Sigmoid – almost never use it, except for the output layer because we want to have the output between 0 and 1

Tanh – use it instead of sigmoid because basically it’s the same functions, but it’s centered in 0, thus helping the gradients to be centered in 0 as the input features; it almost every time works better than the sigmoid

ReLU – it’s the default activation function in deep learning; when the gradients are large / small, this function helps the network to work faster and to avoid the loss of large gradients, that are maximum 1 while using sigmoid and tanh

Leaky ReLU – almost every time works better than the ReLU, because we also propagate gradients that are smaller than 0; some people treat the parameter from this functions as one that has to be tweaked (hyperparameter)

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**Why do you need Non-Linear Activation Functions?**

If we don’t use non-linear activation functions at least in hidden layers, the network, even if it’s extremely deep, cannot learn something complex because in the end the output is a linear combination of the input features

Only for regression problems we can use a linear activation function in the output layer, but we have to use for the rest of the layers non-linear activation functions

**Derivatives of Activation Functions**

We can denote the derivative of g(z) as g’(z)

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Derivative of the Sigmoid function: g’(z) = g(z) \* (1 – g(z))

Derivative of the Tanh: g’(z) = 1 – g(z)^2

Derivative of the ReLU: g’(z) = 0 if z < 0 or 1 if z >= 0; actually, it’s undefined for z = 0, but we can implement it as stated previously

Derivative of the Leaky ReLU: g’(z) = 0.01 if z < 0 or 1 if z >= 0

**Gradient Descent for Neural Networks**

For a neural network with 2 hidden layers, the parameters of the cost function are W[1], b[1], W[2], and b[2]

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In order to apply the gradient descent, we have to repeatedly compute the outputs and the gradients and then to update the parameters of the cost function

The derivatives for W and b are computed in the same way for each layer, the main difference is when it comes to the derivative of Z

**Backpropagation Intuition (Optional)**

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We can denote the dz as da \* g’(z)

**Backpropagation Intuition (Optional)**

If we have a function foo, then the derivative of foo has the same shape as foo

The derivatives for a neural network with 2 layers (for one example):

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**Random Initialization**

If we initialize all the weights of a neural network with a constant value, for example 0, then in one layer, all the neurons with have the same value and will share the same weights even after multiple training epochs

If we want to break this symmetry, we have to initialize the weights randomly, but in this case we can leave the biases initialized with zeros

This isn’t a problem for a logistic regression, because we have one “neuron” we can initialize the weights with 0

Another important aspect is if we use activation functions such as sigmoid and tanh, we want to initialize the weights with random numbers \* 0.001, just to be sure that the propagated values aren’t too big, so that after passed through these activation functions they become 1 all the time

These are the equations of the gradient descent for a neural network with 2 layers

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